

## Worksheet: Present Value

Assume everyone can “borrow” or “lend” at the same interest rate,  $r = 0.06$ . Savers are lenders. “Lending” can take different forms, such as: depositing money in the bank, purchasing a bond, or making a loan directly to a borrower. “Borrowing” also takes various forms, such as taking out a loan from the bank, or selling a bond.

- 1a. If you borrow \$94.34 for one year, how much will you owe in one year?
- 1b. If you know you will receive \$100 in one year, but want to spend the money now, what amount could you borrow today that you would be able to pay off in one year with the \$100 you receive at that time?
- 1c. Which is better, getting \$94.34 today or getting \$100.00 in one year? (Ignore the time and administrative costs of taking out and repaying loans and focus only on the monetary costs.)
- 2a. For this problem only,  $r = 0.04$ . If you know you will receive \$500 in one year, but want to spend the money now, what amount could you borrow today that you would be able to pay off in one year with the \$500 you receive at that time? Note: This problem is asking you to compute the present value of \$500 to be received in one year.
- 2b. What calculation did you perform to calculate the answer to 2a?
- 2c. The amount you’ll receive in one year is \$A. The interest rate, in decimal form, is  $r$ . Write down a formula for the present value of \$A.
- 3a. Redo 2a assuming the interest rate is  $r = 0.08$ .
- 3b. How does an increase in the interest rate affect the present value of a future amount? Explain.
- 4a. (We’re back to  $r = 0.06$ .) You have \$100 today that you will not need to spend for 2 years. If you lend this money for two years at the market interest rate, you will have \$A in two years. Find \$A.
- 4b. What is the present value of \$A to be received in 2 years (where \$A is your answer to 4a)?
- 4c. Write down a formula for the present value of any amount \$A to be received in two years (i.e., the formula should actually include “A” rather than the particular value of “A” you solved for in 4a and used in 4b).
- 5a. Write down a formula for the present value of any amount \$A to be received in 3 years, assuming the market interest rate every year equals  $r$ . (Use “ $r$ ” rather than a particular value like 0.06.)
- 5b. Write down a formula for the present value of any amount \$A to be received in N years.
6. A bond issued by Apple Corporation matures 3 years from today and pays \$1000 at that time. In addition, the bond pays \$50 in one year, \$50 in two years, and \$50 in three years. The most you should pay for this bond is the present value of the stream of payments you would receive from holding this bond. Calculate this amount, assuming  $r = 0.06$ .
7. Let  $Y_t$  denote your income in year  $t$ , where  $t$  is the number of years from the current year. Thus,  $Y_0$  is your income this year (or 0 years from now),  $Y_1$  is your income next year (1 year from now),  $Y_2$  is your income two years from now, and so on. Suppose you work and earn labor income in each of the years 0 through 5 and then retire (and earn no labor income during retirement), and suppose the interest rate, denoted  $r$ , is the same in all years. Write down an expression for the present value of your labor income.